

Question 17

It is known that 96% of train travellers on a certain route had a valid ticket.

A sample of 500 travellers is taken. For samples of 500 travellers, \hat{P} is the random variable of the distribution of sample proportions of travellers **without** a valid ticket.

$\Pr\left(\hat{P} \leq \frac{3}{100}\right)$, when approximated by a normal distribution, is closest to

- A. 0.1269
- B. 0.1333
- C. 0.1513
- D. 0.4991
- E. 0.8731

Question 18

Let $f(x) = x^2$ and $g(x) = \log_e(2 - 4x)$.

The maximal domain of f for the composite function $g(f(x))$ to exist is

- A. $x \in \left(-\infty, -\frac{1}{2}\right)$
- B. $x \in \left(-\infty, -\frac{\sqrt{2}}{2}\right] \cup \left[\frac{\sqrt{2}}{2}, \infty\right)$
- C. $x \in \left(-\infty, -\frac{\sqrt{2}}{2}\right) \cup \left(\frac{\sqrt{2}}{2}, \infty\right)$
- D. $x \in \left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$
- E. $x \in \left[-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right]$

Question 19

The equation $\sin(kx) = 1$ where $x \in [0, 2\pi]$ has **no solutions** when

- A. $k \in R$
- B. $k \in \pi$
- C. $k \in \left[\frac{1}{4}, \infty\right)$
- D. $k \in \left[0, \frac{1}{4}\right]$
- E. $k \in \left(-\frac{3}{4}, 0\right]$